

# SPAUN

Adam Marblestone  
Cognitive Integration Class

# Outline

- Neural Engineering Framework (NEF)
  - Compiling down functions onto connectivities among spiking neuron populations
    - Via an optimization procedure applied to each functional block in the system, as opposed to “learning”
- Semantic Pointer Architecture (SPA)
  - Vector symbolic architectures
- Overall SPAUN cognitive architecture

# Neural Engineering Framework

spiking neural populations

--> represent vectors,  $\mathbf{x}$ , of a specific length

e.g., 500-dimensional vector, several thousand neurons represent it

basis vectors,  $\mathbf{e}$ , randomly assigned to neurons

*nonlinear* encoding of vector onto firing rates:

$$J = \alpha \mathbf{e} \cdot \mathbf{x} + J_{bias}$$

# Neural Engineering Framework

spiking neural populations

--> represent vectors,  $\mathbf{x}$ , of a specific length

e.g., 500-dimensional vector, several thousand neurons represent it

basis vectors,  $\mathbf{e}$ , randomly assigned to neurons

*nonlinear* encoding of vector onto firing rates:

(input current to neuron)

$$J = \alpha \mathbf{e} \cdot \mathbf{x} + J_{bias}$$

neuron model

spikes

The diagram illustrates the process of encoding a vector into firing rates. It starts with the equation  $J = \alpha \mathbf{e} \cdot \mathbf{x} + J_{bias}$ , where  $J$  is the input current to a neuron. An arrow points from  $J$  to the text 'neuron model'. Another arrow points from 'neuron model' to the text 'spikes'.

# Neural Engineering Framework

spiking neural populations

--> represent vectors,  $\mathbf{x}$ , of a specific length

e.g., 500-dimensional vector, several thousand neurons represent it

basis vectors,  $\mathbf{e}$ , randomly assigned to neurons

*linear decoding* by a readout population, via connection weights:

We can also perform the opposite operation: given a sequence of spikes we can estimate the original vector. As shown elsewhere (Eliasmith & Anderson, 2003), this can be done by deriving the decoding vectors  $\mathbf{d}$  as per Equation 2, where  $a_i$  is the average firing rate for neuron  $i$  with a given vector  $\mathbf{x}$ , and the integration is over all values of  $\mathbf{x}$ .

$$\mathbf{d} = \Gamma^{-1} \mathbf{Y} \quad \Gamma_{ij} = \int a_i a_j d\mathbf{x} \quad \mathbf{Y}_j = \int a_j \mathbf{x} d\mathbf{x} \quad (2)$$

**Symbolic Reasoning in Spiking Neurons:  
A Model of the Cortex/Basal Ganglia/Thalamus Loop**

Terrence C. Stewart (tcstewar@uwaterloo.ca)

Xuan Choo (fchoo@uwaterloo.ca)

Chris Eliasmith (celiasmith@uwaterloo.ca)

Centre for Theoretical Neuroscience, University of Waterloo

Waterloo, ON, N2L 3G1

# Neural Engineering Framework

spiking neural populations

--> represent vectors,  $\mathbf{x}$ , of a specific length

e.g., 500-dimensional vector, several thousand neurons represent it

basis vectors,  $\mathbf{e}$ , randomly assigned to neurons

*linear decoding* by a readout population, via connection weights:

$$\hat{\mathbf{x}}(t) = \sum_{i,n} \delta(t - t_{i,n}) * h_i(t) \mathbf{d}_i = \sum_{i,n} h(t - t_{i,n}) \mathbf{d}_i \quad (3)$$

**Symbolic Reasoning in Spiking Neurons:  
A Model of the Cortex/Basal Ganglia/Thalamus Loop**

Terrence C. Stewart (tcstewar@uwaterloo.ca)

Xuan Choo (fchoo@uwaterloo.ca)

Chris Eliasmith (celiasmith@uwaterloo.ca)

Centre for Theoretical Neuroscience, University of Waterloo

Waterloo, ON, N2L 3G1

# Neural Engineering Framework

spiking neural populations

--> represent vectors,  $x$ , of a specific length

e.g., 500-dimensional vector, several thousand neurons represent it

*you can also decode using connection weights with a transformation*

*that transformation can approximate any function*

*optimize the weights to minimize error in that approximation*

*reminiscent of kernel methods:*

*nonlinearly map into high-dim space, then apply linear operators*

**Symbolic Reasoning in Spiking Neurons:  
A Model of the Cortex/Basal Ganglia/Thalamus Loop**

Terrence C. Stewart (tcstewar@uwaterloo.ca)

Xuan Choo (fchoo@uwaterloo.ca)

Chris Eliasmith (celiasmith@uwaterloo.ca)

Centre for Theoretical Neuroscience, University of Waterloo

Waterloo, ON, N2L 3G1

# Neural Engineering Framework

So...

- 1) describe your system in terms of high-dimensional vectors
- 2) describe system functions as transformation on those vectors
- 3) compile onto neurons by randomly choosing input-current basis vectors, then optimizing connection weights

**Symbolic Reasoning in Spiking Neurons:  
A Model of the Cortex/Basal Ganglia/Thalamus Loop**

Terrence C. Stewart (tcstewar@uwaterloo.ca)

Xuan Choo (fchoo@uwaterloo.ca)

Chris Eliasmith (celiasmith@uwaterloo.ca)

Centre for Theoretical Neuroscience, University of Waterloo  
Waterloo, ON, N2L 3G1

# Neural Engineering Framework

So...

- 1) describe your system in terms of high-dimensional vectors**
- 2) describe system functions as transformation on those vectors
- 3) compile onto neurons by randomly choosing input-current basis vectors, then optimizing connection weights

**Symbolic Reasoning in Spiking Neurons:  
A Model of the Cortex/Basal Ganglia/Thalamus Loop**

Terrence C. Stewart (tcstewar@uwaterloo.ca)

Xuan Choo (fchoo@uwaterloo.ca)

Chris Eliasmith (celiasmith@uwaterloo.ca)

Centre for Theoretical Neuroscience, University of Waterloo  
Waterloo, ON, N2L 3G1

# Neural Engineering Framework

symbol binding / compositionality:

circular convolution operation on vectors

**blue⊗circle + red⊗square**

**Symbolic Reasoning in Spiking Neurons:  
A Model of the Cortex/Basal Ganglia/Thalamus Loop**

Terrence C. Stewart (tcstewar@uwaterloo.ca)

Xuan Choo (fchoo@uwaterloo.ca)

Chris Eliasmith (celiasmith@uwaterloo.ca)

Centre for Theoretical Neuroscience, University of Waterloo  
Waterloo, ON, N2L 3G1

# Neural Engineering Framework

symbol binding / compositionality:

circular convolution operation on vectors

$$\begin{aligned} & (\text{blue} \otimes \text{circle} + \text{red} \otimes \text{square}) \otimes \text{red}^* \\ &= \text{blue} \otimes \text{circle} \otimes \text{red}^* + \text{red} \otimes \text{square} \otimes \text{red}^* \\ &\approx \text{blue} \otimes \text{circle} \otimes \text{red}^* + \text{square} \end{aligned}$$

**Symbolic Reasoning in Spiking Neurons:  
A Model of the Cortex/Basal Ganglia/Thalamus Loop**

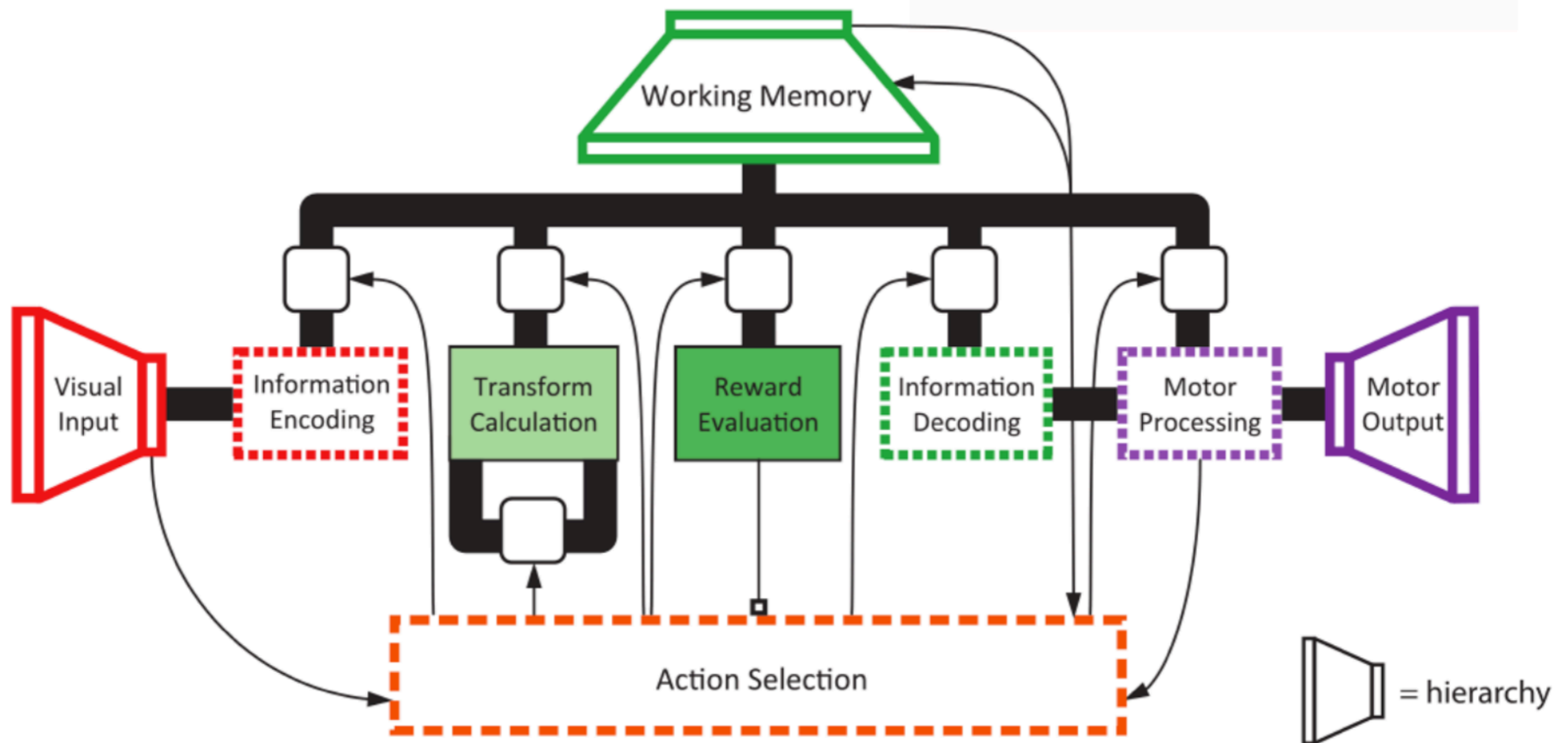
Terrence C. Stewart (tcstewar@uwaterloo.ca)

Xuan Choo (fchoo@uwaterloo.ca)

Chris Eliasmith (celiasmith@uwaterloo.ca)

Centre for Theoretical Neuroscience, University of Waterloo  
Waterloo, ON, N2L 3G1

# Neural Engineering Framework



## A Large-Scale Model of the Functioning Brain

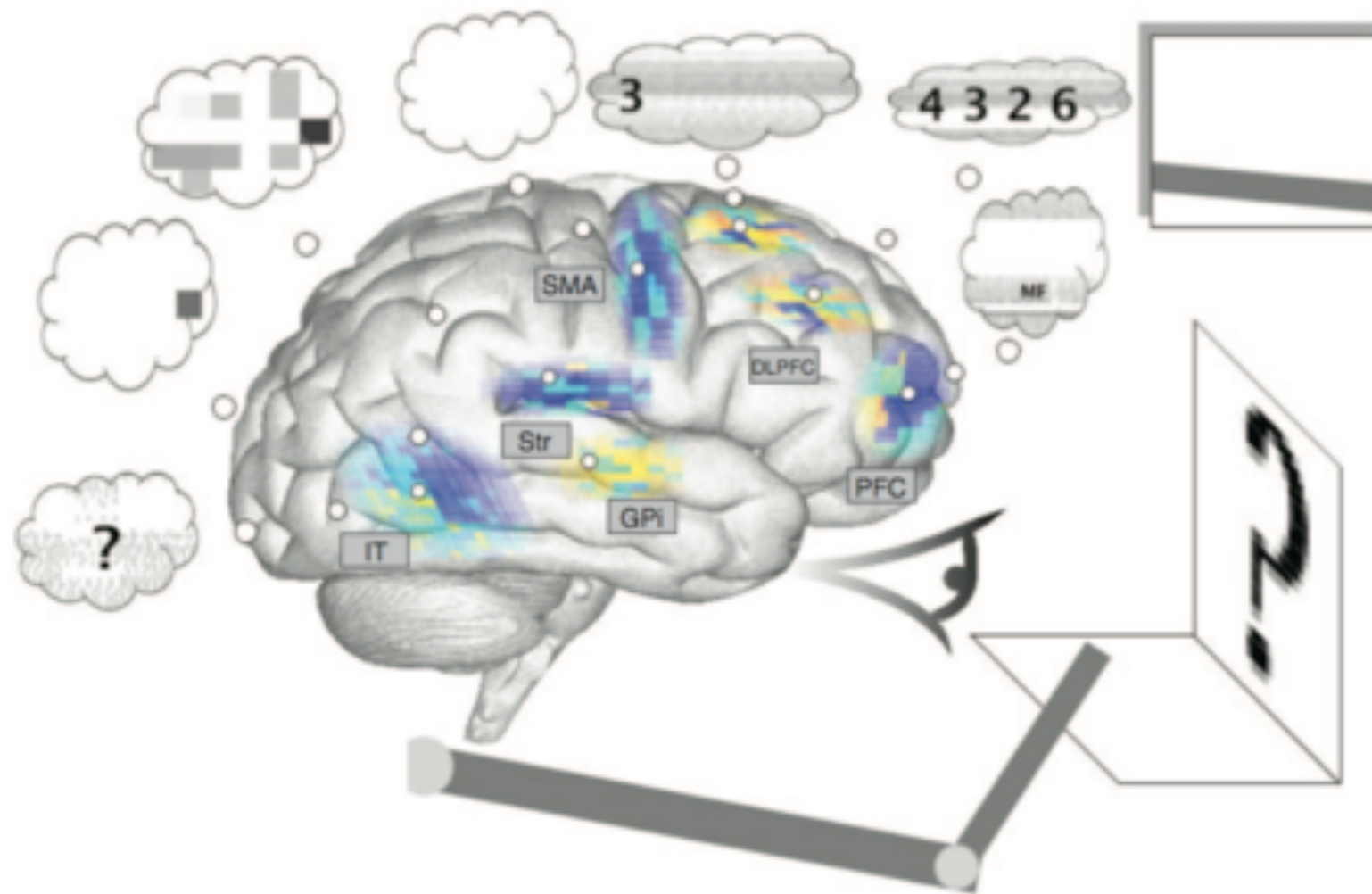
Chris Eliasmith<sup>+</sup>, Terrence C. Stewart, Xuan Choo, Trevor Bekolay, Travis DeWolf, Yichuan Tang, Daniel Rasmussen

<sup>+</sup> Author Affiliations

<sup>↩</sup> To whom correspondence should be addressed. E-mail: [celiasmith@uwaterloo.ca](mailto:celiasmith@uwaterloo.ca)

*Science* 30 Nov 2012:  
Vol. 338, Issue 6111, pp. 1202-1205  
DOI: [10.1126/science.1225266](https://doi.org/10.1126/science.1225266)

# Neural Engineering Framework



## A Large-Scale Model of the Functioning Brain

Chris Eliasmith<sup>+</sup>, Terrence C. Stewart, Xuan Choo, Trevor Bekolay, Travis DeWolf, Yichuan Tang, Daniel Rasmussen

<sup>+</sup> Author Affiliations

<sup>↩</sup> To whom correspondence should be addressed. E-mail: [celiasmith@uwaterloo.ca](mailto:celiasmith@uwaterloo.ca)

*Science* 30 Nov 2012:  
Vol. 338, Issue 6111, pp. 1202-1205  
DOI: [10.1126/science.1225266](https://doi.org/10.1126/science.1225266)

# Neural Engineering Framework

Picking representations and block decomposition and locally optimizing connections

**vs.**

End-to-end optimization / learning

Good picture of a potential end-state of learning?

## A Large-Scale Model of the Functioning Brain

Chris Eliasmith<sup>+</sup>, Terrence C. Stewart, Xuan Choo, Trevor Bekolay, Travis DeWolf, Yichuan Tang, Daniel Rasmussen

<sup>+</sup> Author Affiliations

<sup>✉</sup>To whom correspondence should be addressed. E-mail: [celiasmith@uwaterloo.ca](mailto:celiasmith@uwaterloo.ca)

*Science* 30 Nov 2012:  
Vol. 338, Issue 6111, pp. 1202-1205  
DOI: [10.1126/science.1225266](https://doi.org/10.1126/science.1225266)